Exam. Code : 209003

Subject Code: 4882

M.Sc. Physics 3rd Semester (Batch 2020-22)

ELECTRODYNAMICS—II

Paper—PHY-502

Time Allowed—3 Hours]

[Maximum Marks—100

Note:—Attempt FIVE questions in all, selecting at least
ONE question from each section. The fifth question
may be attempted from any section. All questions
carry equal marks.

SECTION-A

- 1. (a) What are TE and TM modes? Why TEM modes cannot exist inside a hollow waveguide? 4
 - (b) Discuss the propagation of TE modes in a rectangular waveguide. The direction of propagation may be assumed z-axis and the dimensions of the waveguide to be a, b along x and y-axis respectively.
- Starting from Maxwell's equations and boundary conditions for a perfectly conducting hollow waveguide, develop uncoupled wave equations for z- component of electric and magnetic field. "z" is the direction of propagation.

SECTION—B

- 3. (a) What do you understand by covariance and manifest covariance?
 - (b) Represent Maxwell's equations in the language of special theory of relativity. 14
- 4. A parallel plate capacitor has surface charge densities ±σ₀ respectively on its plates. Obtain transformation relation for electric and magnetic field components between two frames of reference moving at a speed "v" with respect to each other.

SECTION—C

5. Verify whether potential

$$V(r, \theta, t) = \frac{p_0 \cos \theta}{4\pi \in_0 r} \left(-\frac{\omega}{c} \sin \left[\omega \left(t - \frac{r}{c} \right) \right] + \frac{1}{r} \cos \left[\omega \left(t - \frac{r}{c} \right) \right] \right)$$

and
$$\vec{A}(r, \theta, t) = -\frac{\mu_0 p_0 \omega}{4\pi r} \sin \left[\omega \left(t - \frac{r}{c}\right)\right] \hat{z}$$
 satisfy

 $\nabla . \vec{A} = -\mu_0 \in_0 \frac{\partial V}{\partial t}$ (the Lorentz Gauge equation). The del operator may be taken as

$$\nabla \cdot \vec{f} = \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 f_r) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \theta} (\sin \theta f_{\theta}) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} (f_{\phi})$$
20

(Contd.)

6. Consider an electric dipole oriented along z-axis, oscillating at frequency "ω". Derive expressions for (a) radiated electric field, (b) radiated magnetic field and (c) Poynting vector. Also determine the total power radiated. Use suitable approximations.

SECTION-D

7. If $V(\vec{r},t) = \frac{q c}{4\pi\epsilon_0(rc - \vec{r}.\vec{v})}$ and $\vec{A}(\vec{r},t) = \frac{\vec{v}}{c^2}V(\vec{r},t)$.

Determine $\vec{E}(\vec{r}, t)$ and $\vec{B}(\vec{r}, t)$. Here \vec{r} and \vec{r} represents the vector connecting origin and observation point and source point and observation point, respectively.

- 8. (a) The Bohr radius of an electron travelling around hydrogen atom is 5 × 10⁻¹¹ m. As per classical electrodynamics, this electron should radiate and hence spiral into the nucleus. Using Larmor formula, show that the electron velocity v is <<c (the speed of light) for most part of the trip.
 - (b) Calculate the life span of the Bohr atom in continuation of part (a).
 - (c) What are Lienard Wiechert potentials and why are they useful?

3